

QUIZ 4 SOLUTIONS: LESSON 2
JANUARY 16, 2019

Write legibly, clearly indicate the question you are answering, and put a box or circle around your final answer. If you do not clearly indicate the question numbers, I will take off points. Write as much work as you need to demonstrate to me that you understand the concepts involved. If you have any questions, raise your hand and I will come over to you.

It is estimated that t hours after 8:00 am, the population of a certain bacterial sample, denoted $N(t)$, will be changing at a rate of

$$N'(t) = \frac{9t}{\sqrt{t+5}} \text{ hundred bacteria/hour.}$$

1. [2 pts] Set up the integral that describes the average change in the bacteria population from 9:00 am to 3:00 pm.

9:00 am is 1 hour past 8:00 am
 3:00 pm is 7 hours past 8:00 am

$$\text{Average} = \frac{1}{7-1} \int_1^7 \frac{9t}{\sqrt{t+5}} dt$$

2. [8 pts] Compute the value of the integral from # 1.

$$\frac{1}{6} \int_1^7 \frac{9t}{\sqrt{t+5}} dt = \frac{9}{6} \int_1^7 t(t+5)^{-1/2} dt$$

$$\begin{aligned} u &= t+5 \Rightarrow t = u-5 \\ \frac{du}{dt} &= 1 \Rightarrow du = dt \\ u(7) &= 7+5 = 12 \\ u(1) &= 1+5 = 6 \end{aligned}$$

$$\begin{aligned} &= \frac{3}{2} \int_{u(1)}^{u(7)} (u-5) u^{-1/2} du \\ &= \frac{3}{2} \int_6^{12} (u^{1-1/2} - 5u^{-1/2}) du \\ &= \frac{3}{2} \int_6^{12} (u^{1/2} - 5u^{-1/2}) du \\ &= \frac{3}{2} \left[\frac{1}{1/2+1} u^{1/2+1} - \frac{5}{-1/2+1} u^{-1/2+1} \right]_6^{12} \\ &= \frac{3}{2} \left[\frac{1}{3/2} u^{3/2} - \frac{5}{1/2} u^{1/2} \right]_6^{12} \\ &= u^{3/2} - 15u^{1/2} \Big|_6^{12} \\ &= \boxed{12^{3/2} - 15\sqrt{12} - [6^{3/2} - 15\sqrt{6}]} \end{aligned}$$